EENG 281 Homework #5 Solutions Fall 2013

P 5.6 [a]
$$i_2 = \frac{150 \times 10^{-3}}{2000} = 75 \,\mu\text{A}$$

 $v_1 = -40 \times 10^3 i_2 = -3 \,\text{V}$
[b] $\frac{v_1}{20,000} + \frac{v_1}{40,000} + \frac{v_1 - v_o}{50,000} = 0$
 $\therefore v_o = 4.75v_1 = -14.25 \,\text{V}$
[c] $i_2 = 75 \,\mu\text{A}$, (from part [a])
[d] $i_o = \frac{-v_o}{25,000} + \frac{v_1 - v_o}{50,000} = 795 \,\mu\text{ A}$

P 5.26 Use voltage division to find v_p :

$$v_p = \frac{2000}{2000 + 8000} (5) = 1 \text{ V}$$

Write a KCL equation at v_n and solve it for v_o :

$$\frac{v_n - v_a}{5000} + \frac{v_n - v_o}{R_f} = 0$$
 so $\left(\frac{R_f}{5000} + 1\right)v_n - \frac{R_f}{5000}v_a = v_o$

Since the op amp is ideal, $v_n = v_p = 1$ V, so

$$v_o = \left(\frac{R_f}{5000} + 1\right) - \frac{R_f}{5000}v_a$$

To satisfy the equation,

$$\left(\frac{R_f}{5000} + 1\right) = 5$$
 and $\frac{R_f}{5000} = 4$

Thus, $R_f = 20 \text{ k}\Omega$.

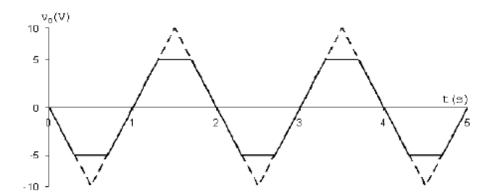
P 5.36 It follows directly from the circuit that $v_o = -(120/7.5)v_g = -16v_g$ From the plot of v_g we have $v_g = 0$, t < 0

$$\begin{array}{rclcrcl} v_g & = & t & 0 \leq t \leq 0.5 \\ \\ v_g & = & 1-t & 0.5 \leq t \leq 1.5 \\ \\ v_g & = & t-2 & 1.5 \leq t \leq 2.5 \\ \\ v_g & = & 3-t & 2.5 \leq t \leq 3.5 \\ \\ v_q & = & t-4 & 3.5 \leq t \leq 4.5, & \text{etc.} \\ \end{array}$$

Therefore

$$v_o = -16t$$
 $0 \le t \le 0.5$
 $v_o = 16t - 16$ $0.5 \le t \le 1.5$
 $v_o = 32 - 16t$ $1.5 \le t \le 2.5$
 $v_o = 16t - 48$ $2.5 \le t \le 3.5$
 $v_o = 64 - 16t$ $3.5 \le t \le 4.5$, etc.

These expressions for v_o are valid as long as the op amp is not saturated. Since the peak values of v_o are ± 5 , the output is clipped at ± 5 . The plot is shown below.



$$\begin{split} \text{P 5.39} \quad \text{[a]} \ \, p_{16\,\text{k}\Omega} &= \frac{(320\times 10^{-3})^2}{(16\times 10^3)} = 6.4\,\mu\text{W} \\ \text{[b]} \ \, v_{16\,\text{k}\Omega} &= \left(\frac{16}{64}\right)(320) = 80\,\text{mV} \\ \\ p_{16\,\text{k}\Omega} &= \frac{(80\times 10^{-3})^2}{(16\times 10^3)} = 0.4\,\mu\text{W} \end{split}$$

[c]
$$\frac{p_{\rm a}}{p_{\rm b}} = \frac{6.4}{0.4} = 16$$

- [d] Yes, the operational amplifier serves several useful purposes:
 - First, it enables the source to control 16 times as much power delivered to the load resistor. When a small amount of power controls a larger amount of power, we refer to it as *power amplification*.
 - Second, it allows the full source voltage to appear across the load resistor, no matter what the source resistance. This is the *voltage* follower function of the operational amplifier.
 - Third, it allows the load resistor voltage (and thus its current) to be set without drawing any current from the input voltage source. This is the *current amplification* function of the circuit.